

# Mathematical modeling of extracorporeal CO<sub>2</sub> removal

Bilans de matière

$$\begin{aligned} Atot &= HA + A- \\ BB &= HC + H- \\ Rt_{\dot{O}2} &= RO_{\dot{O}2} + r_{\dot{O}2} \end{aligned}$$

Equilibres acido-basique

$$\begin{aligned} H^+ &= K_{HCO_3^-} \cdot \frac{CO_2}{HCO_3^-} \\ H^+ &= K_a \cdot \frac{HA}{A^-} \\ H^+ &= K_w \cdot \frac{H_2O}{OH^-} = K'_w \cdot \frac{1}{OH^-} \\ H^+ &= K_d \cdot \frac{HCO_3^-}{CO_3^{2-}} \\ H^+ &= K_{RCOO^-} \cdot \frac{RCOOH}{RCOO^-} \end{aligned}$$

Propriétés physico-chimiques

$$CO_2 = \alpha P_{CO_2}$$

$$\begin{aligned} V_{A,CO_2} \cdot \dot{P}_{a,CO_2}(t) &= 863 \cdot Q_P \cdot (\bar{C}_{v,CO_2}(t - \tau_P) - \bar{C}_{a,CO_2}(t)) + \dot{V}_A \cdot (P_{I,CO_2} - P_{a,CO_2}(t)) \\ V_{A,O_2} \cdot \dot{P}_{a,O_2}(t) &= 863 \cdot Q_P \cdot (\bar{C}_{v,O_2}(t - \tau_P) - \bar{C}_{a,O_2}(t)) + \dot{V}_A \cdot (P_{I,O_2} - P_{a,O_2}(t)) \\ V_{T,O_2} \cdot \dot{C}_{v,O_2}(t) &= Q_S \cdot (\bar{C}_{a,CO_2}(t - \tau_T) - \bar{C}_{v,CO_2}(t)) - MR_{CO_2} \\ &\quad + MR_{O_2} \end{aligned}$$

# Introduction

*Pulmonary insufficiency*



*Intensive care unit*



- ❖ Severe pulmonary diseases
  - Ventilator
  - ECLS
- ❖ Protective ventilation
  - High FIO<sub>2</sub>
  - High respiratory frequency
  - Low tidal volume
  - ⇒ High pCO<sub>2</sub>
  - ⇒ blood acidosis

# Introduction

*Pulmonary insufficiency*



*Intensive care unit*



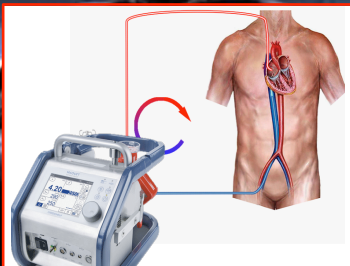
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    - Ventilator
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    - High FIO<sub>2</sub>
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    - Low tidal volume
    - ⇒ High pCO<sub>2</sub>
    - ⇒ blood acidosis
  - ❖ ECCO<sub>2</sub>R = vv-ECLS with low blood flow
  - ❖ ECCO<sub>2</sub>R => pCO<sub>2</sub> decrease
  - ❖ The goal: decrease the pCO<sub>2</sub> rapidly with small canula
- ⇒ Find an optimal blood flow across the device

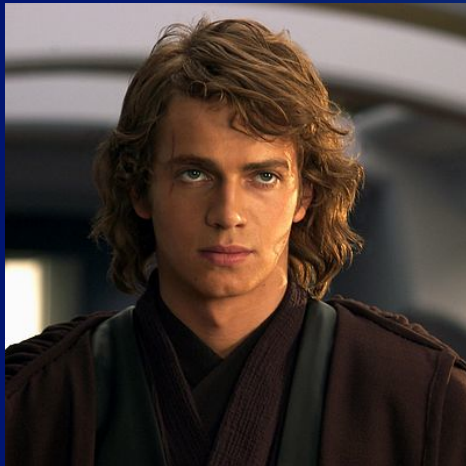


# Introduction

*Pulmonary insufficiency*



*Intensive care unit*



**Recovery**

❖ Severe pulmonary diseases

- Ventilator
- ECLS

❖ Protective ventilation

- High FIO<sub>2</sub>
- High respiratory frequency
- Low tidal volume

⇒ High pCO<sub>2</sub>

⇒ blood acid

ECCO<sub>2</sub>R = v low blood flow

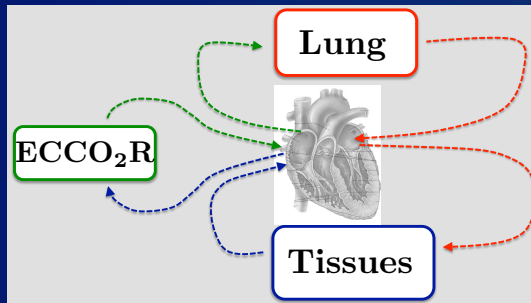
ECCO<sub>2</sub>R => e

The good canula rapidly with small



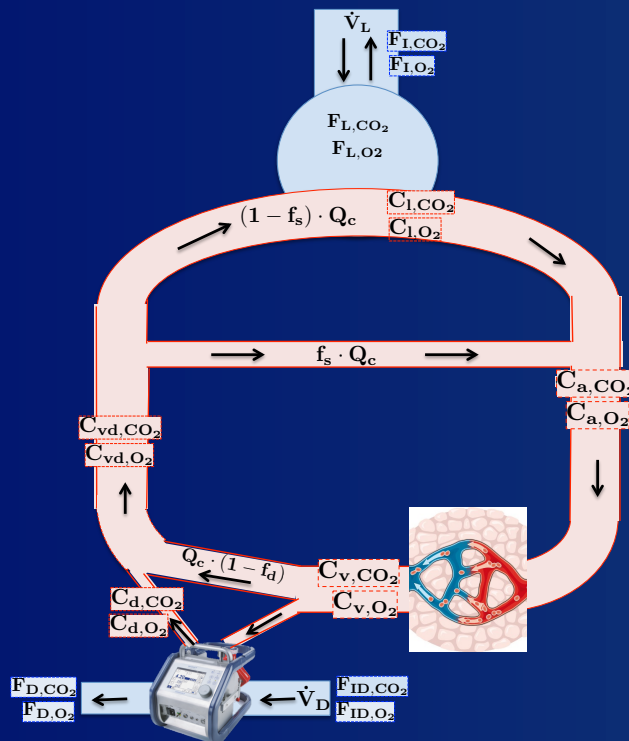
⇒ Find an optimal blood flow across the device

# Methods



## ❖ Lumped parameters model with 3 compartments

- Lung
- Tissues
- ECCO<sub>2</sub>R device



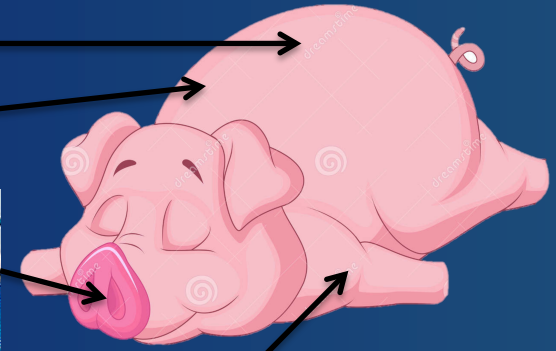
## ❖ The mathematical model considers

- Pulmonary shunt
- Equilibrium between alveoli and pulmonary capillaries

❖ Validation = predictions of the model vs experimental data.

❖ Data:

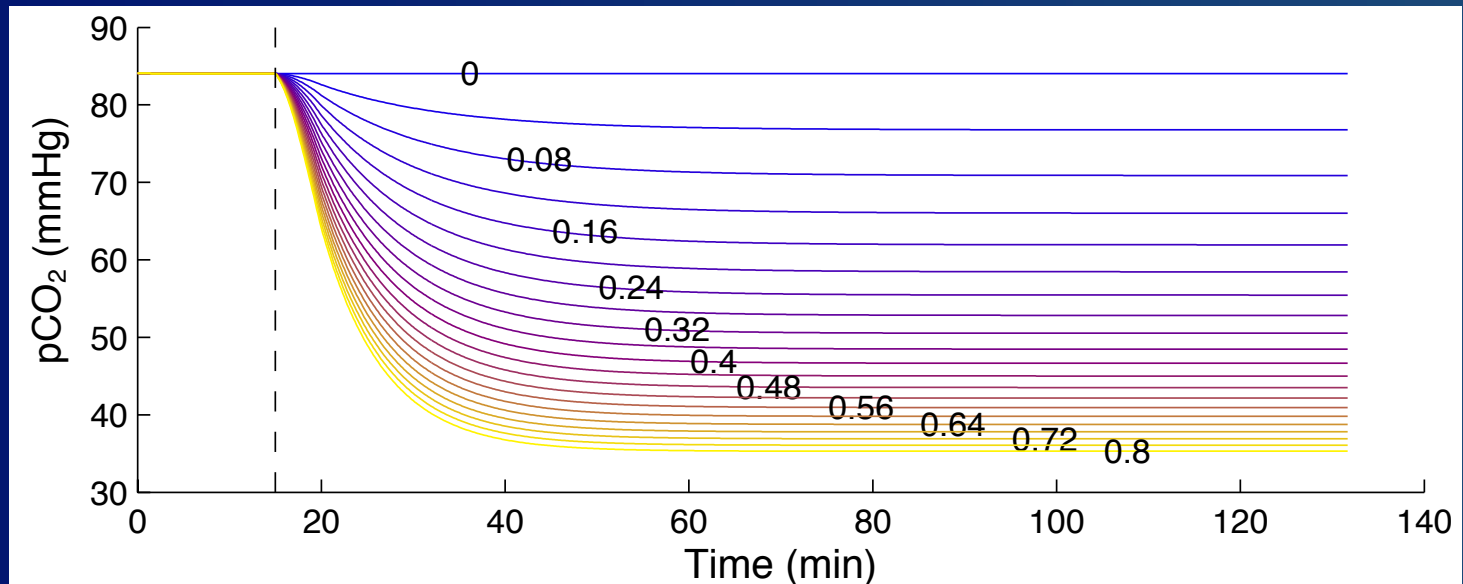
- Weight
- Cardiac output
- Tidal volume
- Respiratory frequency
- Arterial and venous blood samples



=>The mathematical simulation is specific to the subject

# Results

## ❖ Blood flow sensibility



- ❖ Decrease is faster for large values of the flow
- ❖ 0.6 l/min seems to be a good compromise.
- ❖ First step towards an **optimized clinical use of ECCO<sub>2</sub>R.**





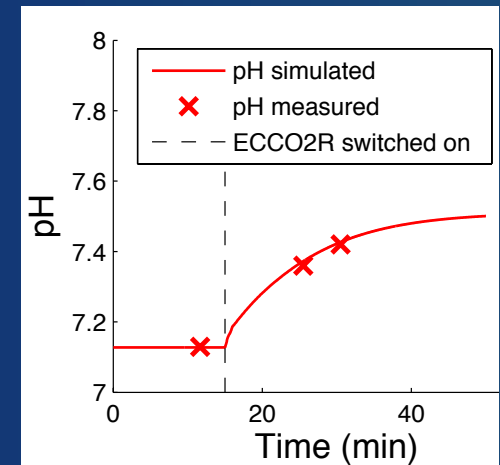
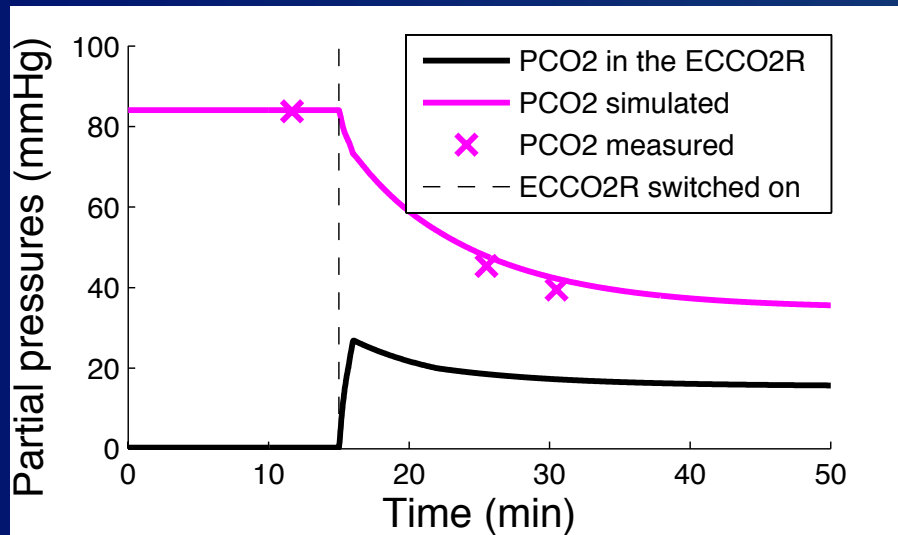
Thank you for your attention

My poster will be shown in gold room SaBPoT4.8  
on Saturday morning at 10:00-11:30



# Additional results

## ❖ Validation



❖ Good agreements between the experimental and calculated time evolution of  $p\text{CO}_2$  and pH in arteries